

# **HKUST Dual Program 2024** (Introduction to Pre-stage Level: Mathematics)

7 September 2024 (Sat)

## Aims of Pre-stage Level

- Equip students with basic and fundamental mathematics knowledge and techniques (mostly in Algebra) for learning elementary Calculus
- Build up good foundation of mathematics for "Level 1" onwards
- Develop appreciation of mathematics from different perspectives
- Present mathematical ideas logically



# **About Pre-stage (MATH) Course**

### Content:

Mainly based on selected topics of **HKDSE Core Mathematics**, with some **additional topics and applications** delivered

### **Course Instructors:**

Dr. Kwun Lun Alan <u>CHU</u> (Class A, English) Mr. Hoi Sang <u>KONG</u> (Class B, Chinese)

### Common Lecture Notes (in English) will be used for all classes

### **Duration:**

16 "3-hour lectures" plus 2 "3-hour tutorials", Saturdays of Nov 2024 – May 2025 (2:00 pm – 5:00 pm)

### **Pre-requisites\*:**

Basic understanding of **elementary Algebra** Certain **mathematical maturity / related experience** will be a bonus \* From 2022/23 onwards, all Pre-stage applicants are required to sit for a <u>screening test</u>.

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# **About Pre-stage Course**

## **Assessment:**

Several HWs (30%) 1 Midterm Examination (30%) 1 Final Examination (40%) \*Outstanding students will be promoted to DP Level 1.

### **Topics Covered:**

- Numbers and Basic Algebra
- Polynomials and Binomial Theorem
- Functions and its Geometric Representations
- Coordinate Geometry
- Trigonometric Formulae
- Sequences and Series





# **Brief Descriptions of Topics**

**Numbers and Basic Algebra:** Basic Set Theory and Number System, Division Algorithm, Mathematical Induction, Proof by Contradiction etc.

**Polynomials and Binomial Theorem:** Algebra of Polynomials, Partial Fraction Decomposition, Factor and Remainder Theorem, Binomial Theorem

### **Functions and its Geometric Representations:**

Definition of a Function, Graphs of a Function, Trigonometric Functions and some Geometric applications

**Coordinate Geometry:** Coordinate System, Geometric Transformation (e.g., Translation and Rotation)



Mathematical Induction









# **Brief Descriptions of Topics**

- 1=1
- 1+3=4=2<sup>2</sup>
- 1+3+5=9=3<sup>2</sup>
- $1+3+5+11+13+15=36=6^2$

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- $1+3+5+...+(2k-1)=(k)^2$  ?
- How to prove it ?

Mathematical Induction



# **Brief Descriptions of Topics**

**Trigonometric Formulae:** Trigonometric Functions on the Coordinate Plane, Compound Angle Formula, Sum to Product / Product to Sum, Half Angle Formula

#### **Sequences and Series:**

Arithmetic Sequence and Series Geometric Sequence and Series Daily Life Applications and Usage



Sum to Product Formulas



$$\sin A + \sin B = 2 \sin \left(\frac{A+B}{2}\right) \cos \left(\frac{A-B}{2}\right)$$
$$\sin A - \sin B = 2 \sin \left(\frac{A-B}{2}\right) \cos \left(\frac{A+B}{2}\right)$$
$$\cos A - \cos B = -2 \sin \left(\frac{A+B}{2}\right) \sin \left(\frac{A-B}{2}\right)$$
$$\cos A + \cos B = 2 \cos \left(\frac{A+B}{2}\right) \cos \left(\frac{A-B}{2}\right)$$



## Focus of Pre-stage Level (MATH)

Although we will have a lot of <u>computations</u> during this course, we also emphasize on the followings:

- 1. Logical Thinking and Mathematical Derivation
- 2. The ways of presenting proper mathematical proofs and explanations in a more professional manner





"I think you should be more explicit here in step two."